



Daffodil International University

Department of Software Engineering

Faculty of Science & Information Technology

Midterm Examination, Fall 2024

Course Code: MAT102; Course Title: Mathematics II

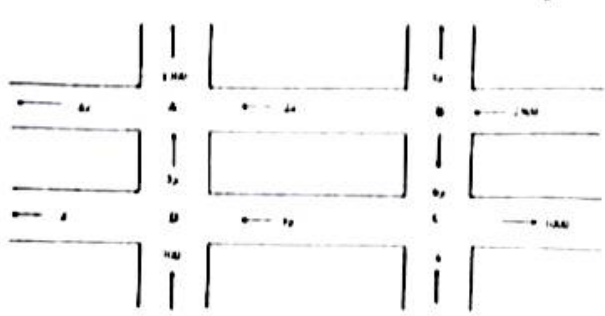
Sections: 42 (All)

Time: 1 Hour 30 Minutes

Marks: 25

Answer ALL Questions

[The figures in the right margin indicate the full marks and corresponding course outcomes. All portions of each question must be answered sequentially]

1.	Explain Identity, Permutation, Involuntary, Symmetric and Hermitian matrix with an example.	5×1=5	CLO-1 L-2
2.	a. Analyze the nature of the trace of a completely non-zero Skew-Hermitian matrix. b. Analyze the relation between the inverse of an orthogonal matrix with its transpose. c. Analyze the rank of the matrix $25I_{150}$.	3×1=3	CLO-2 L-4
3.	$A = \begin{pmatrix} 2 & 1 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 3 & 1 & 2 & 3 \\ 1 & 6 & 1 & 3 \\ 6 & 0 & 1 & 1 \end{pmatrix}$ $B = \begin{pmatrix} 1 & 5 & -3 \\ 3 & 1 & 0 \\ 4 & 2 & 7 \end{pmatrix}$ $B = \begin{pmatrix} 1 & 5 & -3 \\ 3 & 1 & 0 \\ 4 & 2 & 7 \end{pmatrix}$ a. Compute $ B $ by using the cofactor method along 2 nd column. b. Construct the inverse matrix of B , and verify it. c. Determine the rank of A .	$ B = \begin{vmatrix} 1 & 5 & -3 \\ 3 & 1 & 0 \\ 4 & 2 & 7 \end{vmatrix}$ $= 1(7-12) - 5(21-28) - 3(21-4)$ $= -5 + 35 - 45 = -15$ $B^{-1} = \frac{1}{-15} \begin{pmatrix} 7 & -12 & 1 \\ 21 & -28 & 3 \\ 21 & -4 & -5 \end{pmatrix}$ $= \begin{pmatrix} -\frac{7}{15} & \frac{4}{5} & -\frac{1}{15} \\ -\frac{7}{5} & \frac{28}{15} & -\frac{1}{5} \\ -\frac{7}{5} & \frac{4}{15} & \frac{1}{3} \end{pmatrix}$	CLO-3 L-3
Answer question 4 and 5 based on the following: The following diagram describes the traffic flow of a congested area of a city on some day. 			
4.	Illustrate the system of linear equations from the above scenario.	2	CLO-3 L-3
5.	Figure out the solution of the system for unknown flow rates.	5	CLO-4 L-4